We present the results of a search for low energy $\bar{\nu}_e$ from the Sun using 1496 days of data from Super-Kamiokande-I. We observe no significant excess of events and set an upper limit for the conversion probability to $\nu_e$. This conversion limit is $0.8\%$ (90\% C.L.) of $\nu_e$ from the Sun at Super-Kamiokande-I.

Solar neutrino measurements at Super-Kamiokande [1] and SNO [2] have established that the solar neutrino problem is explained by the transformation of electron neutrinos to other active neutrinos. The mechanism for...
this transformation is generally assumed to be via neutrino flavor oscillations from $\nu_\mu$ to some superposition of $\nu_\mu$ and $\nu_\tau$. However, measurements reported so far do not rule out the possibility that some of the $\nu_\tau$ transform to antiparticles ($\bar{\nu}_\mu$, $\bar{\nu}_\tau$). In the so-called “hybrid models” [3], spin flavor precession (SFP) and oscillation can transform solar neutrinos to $\bar{\nu}_e$ if the neutrino is Majorana, it has large magnetic moment, and the Sun has a large magnetic field. If the neutrino has a magnetic moment, there are two conversion scenarios: the neutrino is a Dirac particle or a Majorana particle. In the Dirac neutrino case, $\nu_e^L$ changes to $\nu_H^R$ by spin magnetic moment transition. The $\nu_e^R$ is a sterile neutrino. On the other hand, in the case of the Majorana neutrino, SFP causes $\nu_e \rightarrow \bar{\nu}_\mu, \tau$. Neutrino oscillation then yields $\bar{\nu}_\mu, \tau \rightarrow \bar{\nu}_e$. Solar $\bar{\nu}_e$ could also originate from neutrino decay [4]. In this paper, we present a search for $\bar{\nu}_e$ from the Sun.

The inverse beta decay process, $\bar{\nu}_e + p \rightarrow n + e^+$ is predominant for $\bar{\nu}_e$ interaction in Super-Kamiokande (SK). The positron energy is related to the neutrino energy by: $E_{\nu e} = E_{e^+} - 1.3$ MeV. The positron angular distribution relative to the incident $\bar{\nu}_e$ direction is nearly flat with a small energy dependent slope [5], which is in contrast to the sharply forward peaked elastic scattering distribution. The difference between these distributions can be used to separate solar neutrino events from $\bar{\nu}_e$ events.

Super-Kamiokande is a 22.5 kton fiducial volume water Cherenkov detector, located in the Kamioka mine in Gifū, Japan. The 1496 live days of solar neutrino data from Super-Kamiokande-I were collected between May 31, 1996, and July 15, 2001. A detailed description of SK can be found elsewhere [4, 5]. The dominant background to the solar neutrino signal are $^{222}$Rn in the water, external gamma rays and muon-induced spallation products. Background reduction is carried out in the following steps: first reduction, spallation cut, second reduction, and external $\gamma$-ray cut. The first reduction removes events from electronic noise and other nonphysical sources, and events with poorly reconstructed vertices. The spallation cut removes events due to radio-isotopes (X) produced by cosmic ray muon interactions with water: $\mu + ^{16}O \rightarrow \mu + X$. These radio-isotopes are called “spallation products.” The spallation products have lifetimes from 0.001 to 14 sec, and emit $\beta$ and $\gamma$ rays. We cut these events using likelihood functions based on time, position, and muon pulse height. The time and position likelihood functions are measures of the proximity of a candidate event to a muon track, while the pulse height likelihood function measures the likelihood that a muon produced a shower. These three likelihood functions are used together to discriminate against spallation events [5]. The second reduction removes events with poor vertex fit quality and diffuse Cherenkov ring patterns, both characteristics of low-energy background events. The external $\gamma$-ray cut removes events due to $\gamma$-rays from the surrounding rock and PMTs etc. Fig. 1 shows the energy spectrum after each reduction step.

At SK, a positron from inverse beta decay is indistinguishable from an electron or gamma ray because the delayed 2.2 MeV gamma ray from $n + p \rightarrow d + \gamma$ is below the detector’s energy threshold. In order to remove elastic scattering events due to solar neutrinos, we cut events with $\cos \theta_{\text{sun}} \geq 0.5$, where $\theta_{\text{sun}}$ is the event direction with respect to the direction from the Sun. The region $\cos \theta_{\text{sun}} < 0.5$ would be occupied by solar $\bar{\nu}_e$ event, in addition to known background sources which could not be removed by the standard data reduction. For $E \lesssim 8$ MeV most background events are due to radioactivity in the detector materials (such as $^{222}$Rn). Spallation accounts for a small fraction of background events in this region. In contrast, for $E \gtrsim 8$ MeV, most background events are produced by spallation.

The spallation cut used in the data reduction efficiently removes short-lifetime spallation products. This cut also removes $\sim 90\%$ of long-lifetime products such as $^{16}$N ($\tau_4^N = 7.1$ sec) and $^{14}$Be ($\tau_2^{14}\text{Be} = 13.8$ sec). Event by event removal of the remaining $\sim 10\%$ of these events is impractical because this introduces large dead time. However, we can estimate the contribution of such events to the post-reduction data sample using a statistical subtraction technique. First, we made a time distribution of muon events preceding each low energy event by up to 200 seconds (Fig. 2(A)). Since the average muon rate at SK is $\approx 2.5$ Hz, there is an average of $\approx 500$ events for each low energy event. If the low energy event is due to a long lifetime spallation product, its event time will be correlated with one of the $\sim 500$ preceding muon events. If this is not the case, then its event time will be uncorrelated with all of the muon events. To estimate the number of $\mu$ responsible for spallation events, we have to subtract the number of $\mu$ which did not make spallation events from this distribution. In order to perform this subtraction, we made a sample of artificial events.
distributed randomly in space and time. We applied the spallation cut to the random events as in the actual data sample in order to account for biases introduced by this cut. The muon time distribution of the random sample is shown in Fig. 3(B). The dip near Delta-T = 0 is due to the accidental loss of events by the spallation cut. To estimate the number of muons which made spallation products, distribution (B) with suitable normalization is subtracted from distribution (A). The number of muon events in the delta-T = 100 sec - 200 sec region is used as a normalization factor because the contamination from events in the delta-T = 100 sec - 200 sec region is used as subtracted from distribution (A). The number of muon products, distribution (B) with suitable normalization is to estimate the number of muons which made spallation due to the accidental loss of events by the spallation cut.

The energy spectrum of the solar $\bar{\nu}_e$ is not known because the mechanism for $\bar{\nu}_e$ creation is not known. Even if one assumes the SFP-oscillation hybrid model, the energy spectrum depends on $\mu_e \times B_{\text{Solar}}, \delta m^2$ and $\sin^2(2\theta)$, none of which is known precisely, if at all. In order to deal with this ambiguity, we have chosen two spectrum models: the $^8$B neutrino spectrum and monochromatic (spectrum independent analysis).

For the $^8$B spectrum dependent analysis, we obtain an upper limit on the solar $\bar{\nu}_e$ flux by comparing the observed number of events outside of the elastic scattering peak ($\cos \theta_{\text{sun}} \leq 0.5$) with the expected number of $\bar{\nu}_e$ events assuming that all $^8$B neutrinos convert to $\bar{\nu}_e$. The expected number is obtained by Monte Carlo simulation of solar $\bar{\nu}_e$ interaction with the detector. The SSM $^8$B neutrino flux was assumed ($5.05 \times 10^6$ /cm$^2$/sec). The solid lines in Fig.4 show 90% C.L. limits on the $\bar{\nu}_e$ flux before statistical spallation subtraction. The dashed lines show the limits after statistical subtraction (only for $E \geq 8$ MeV). The combined upper limit for 8 MeV $\leq E \leq 20$ MeV is 0.8% of the SSM neutrino flux.

Some authors have indicated that the positron angular distribution may be useful for the search for $\bar{\nu}_e$ in the SK data (e.g. [1, 11]). Taking $\theta$ as the opening angle between the positron and neutrino momenta, $\cos \theta$ is distributed as $f(\cos \theta) = 0.5 \times (1 + \alpha \times \cos \theta)$, where $\alpha$ is a monotonically increasing function of neutrino energy (except near threshold), and $\alpha \leq 0$ for $E_{\nu} \lesssim 13$ MeV and $\geq 0$ above this [11]. At the lowest neutrino energies, $f(\cos \theta)$ has sufficient slope to be useful for the $\bar{\nu}_e$ search. $\bar{\nu}_e$ events with the predicted $\cos \theta$ distribution were input to a detector simulator to obtain the expected positron angular distribution. The resulting distribution has the same form as above. The fitted value of $\alpha$ is -0.076 at $E_{\text{total}} = 5 - 6$ MeV, 0.107 at $E_{\text{total}} = 12 - 20$ MeV, and crosses 0 at $\sim 9$ MeV.
Solar neutrino elastic scattering is one of the backgrounds for this analysis. Almost all such events have \( \cos \theta_{\text{sun}} > 0.5 \), so events with \( \cos \theta_{\text{sun}} > 0.5 \) are cut. We also subtract the small amount of spill-over into \( \cos \theta_{\text{sun}} \leq 0.5 \) using Monte Carlo simulation (\( \sim 5\% \) for 5-20 MeV). Another background is due to \( 18^O(\nu_e,e)18^F \) [1]. There is only a small number of events from this source (0.03\% \( \sim 2\% \), depending on energy), but electrons from this process, like the low-energy \( \bar{\nu}_e \), have negative slope in their angular distribution. So they are subtracted from the data. The \( \nu_e \) flux is taken as the charged current flux value from SNO, \( 1.76 \times 10^6 / \text{cm}^2/\text{sec} \) [2].

A \( \bar{\nu}_e \) upper limit is obtained using a probability test with the slope of the \( \cos \theta \) distribution serving as a constraint. This test is based on a \( \chi^2 \) test with \( \chi^2 \) defined as follows:

\[
N_{\cos}(=30) = \sum_{i=1}^{N_{\cos}} \left\{ \frac{N_{i}^{\text{data}} - N_{i}^{\text{el}} - N_{i}^{18^O} - \alpha N_{i}^{\bar{\nu}_e} - \beta N_{i}^{BG}(1 + \gamma \cos \theta_{\text{sun}})}{\sigma_{i}^{\text{stat.}}} \right\}^2 + \left( \frac{\gamma}{\sigma_{\gamma}^{\text{syst.}}} \right)^2
\]

\( N_{\cos} \) is the number of angular bins for \( \cos \theta_{\text{sun}} \leq 0.5 \), \( N_{i}^{\text{data}} \) is the number of observed data events, \( \sigma_{i}^{\text{stat.}} \) is the statistical error of the observed data, \( N_{i}^{\text{el}} \) is the expected number of elastic scattering events, \( N_{i}^{18^O} \) is the expected number of events from the \( 18^O(\nu_e,e)18^F \) reaction, \( N_{i}^{\bar{\nu}_e} \) is the number of \( \bar{\nu}_e \) events, \( N_{i}^{BG} \) is the number of all other background events that are uncorrelated in direction with the Sun. \( N_{i}^{\text{el}} \) and \( N_{i}^{18^O} \) are both \( \lesssim 2\% \) of \( N_{i}^{\text{data}} \), and the systematic errors of these terms are negligible. \( \sigma_{\gamma}^{\text{syst.}} \) is the systematic error of the shape of the background and \( \gamma \) is the parameter that takes this into account. \( \beta \) parameterizes the amount of such background events. We selected \( \beta \) and \( \gamma \) which minimizes \( \chi^2 \) for each \( \alpha \). A 1-parameter \( \chi^2 \) is input to a probability function. From this analysis, we set a 90\% C.L. upper limit for each energy bin. The dotted lines in Fig. 4 show the result.

The analysis above assumes that the \( \bar{\nu}_e \)'s originate from \( 8^B \) solar neutrinos. We also generalized our search by assuming a monochromatic \( \bar{\nu}_e \) source at each energy and set a conservative \( \bar{\nu}_e \) flux upper limit. The interaction of such \( \bar{\nu}_e \) with the detector was simulated, and standard data reduction cuts were applied. The positron spectrum is well described by a Gaussian. We then counted the number of events in the data in the \( \pm 1\sigma \) range of this Gaussian. We took this number to be the number of events due to monochromatic \( \bar{\nu}_e \), and we obtained an upper limit. This upper limit is very conservative because we do not take account of the large spill-over from lower energy bins that is implied by the sharply falling spectrum seen in the data. We also obtained limits after statistical subtraction of long lifetime spallation events. The 90\% C.L. limits are shown in Fig. 5.

![Graph](image)

**FIG. 4: Summary of \( \bar{\nu}_e \) limits.** The horizontal axis shows total positron energy in MeV and the vertical axis shows the 90\% C.L. \( \bar{\nu}_e \) rate normalize to the SSM \( \nu_e \) rate. The solid lines show the 90\% C.L. limit ratio. The dashed lines show the limit after statistical subtraction of the spallation background. The dotted lines show the result from the angular distribution analysis.

In summary, a search for \( \bar{\nu}_e \) flux from the Sun was performed using all 1496 live days of solar neutrino data from Super-Kamiokande-I. Using the \( 8^B \) and monochromatic energy spectra, 90\% C.L. upper limits were set for the solar \( \nu_e \) flux. For the \( 8^B \) spectrum, the upper limit to the flux was 0.8\% of the SSM \( \nu_e \) flux prediction for \( E_{\text{total}} = 8.0-20.0 \text{ MeV} \). This can be compared with the Kamiokande result of 4.5\% [3]. For \( \bar{\nu}_e \) fluxes with various monochromatic energies, the resulting upper limits are shown in Fig. 5.

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FIG. 5: $\bar{\nu}_e$ flux 90% C.L. upper limit for each monochromatic $\bar{\nu}_e$. The horizontal axis shows neutrino energy in MeV and the vertical axis shows the flux limit (in /cm$^2$/sec). The black circles show the limits before spallation subtraction while the black stars show the limits after subtraction. The two highest-energy bins have insufficient number of events for statistical subtraction.

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